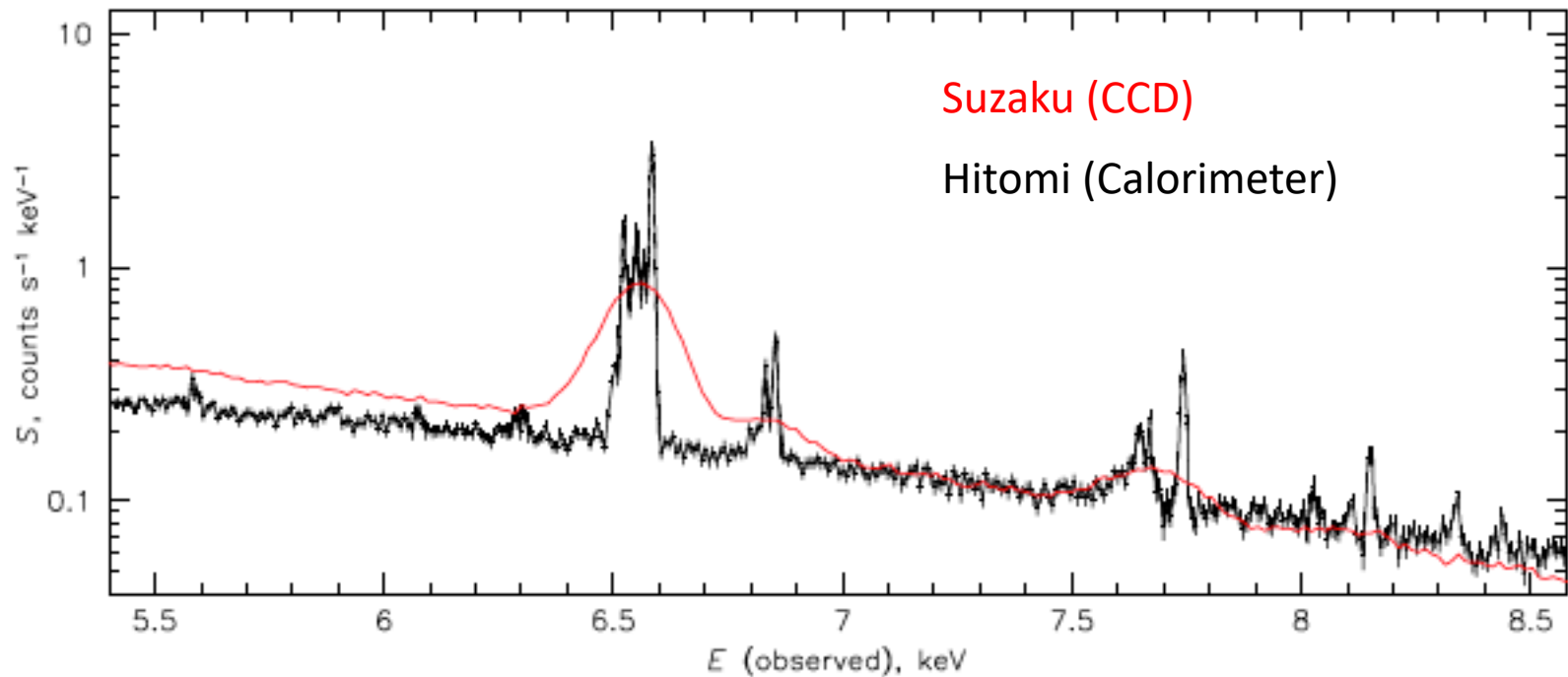


# Atomic data and models: a primer for high resolution X-ray spectroscopy

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# Why care about atomic data?



We see them, and:  
there is information in these lines!

# Preference for black box?



You can use models (APEC, SPEX, Chianti, XSTAR, ...) as black boxes

It gives you a temperature, an abundance

But what does it mean?

How accurate is it?

Why do I see residuals?

Help!



# What can you learn from a spectrum?

1. (Electron) **temperature** (from continuum or lines present)
2. **Ion temperature** (from line broadening)
3. **Turbulence** (from line broadening)
4. **Velocity** fields (from Doppler shifts)
5. Electron **density** (from line ratios)
6. **Emission measure**  $n^2V$  (from flux)
7. **Abundances** (from relative line intensities)
8. **Age** of the plasma (for transient plasmas)
9. **Ionisation process** (photons, electrons)
10. **Nonthermal electrons**
11. **Dust**
12. Sometimes: **magnetic** fields
13. Etc.

# Steps in understanding a thermal spectrum and how to calculate a model for it

1. Basic physical properties:
  - temperature, density, composition, size, shape, influx, .....
2. Determine ionization balance: how many ions of each species
  - depends on physical conditions
3. Calculate emitted spectrum
4. Calculate absorption by the source:  
can all radiation escape?

# Types of plasma

- Type determined by role of collisions of ions with:
  - *Electrons* (always there)
  - *Photons* (relevant for several interesting sources)
  - *Protons* (usually small corrections)
  - *Other ions / atoms* (Charge exchange)
- Always solve balance ionisation  $\leftarrow \rightarrow$  recombination
- Sometimes solve balance heating  $\leftarrow \rightarrow$  cooling
- Sometimes consider transient plasmas

# Ionisation balance

Plasma type	Ionisation Balances recombination	Heating balances cooling	Time dependent (no balance)	Optical depth
<b>CIE</b> (Collisional Ionisation Equilibrium)	✓	✗	✗	$\tau=0$
<b>PIE</b> (Photo Ionisation Equilibrium)	✓	✓	✗	$\tau>1$
<b>NEI</b> (Non-Equilibrium Ionisation)	✓ With source term	✗	✓	$\tau=0$
<b>Transient PIE</b>	✓ With source term	?	✓	$\tau>1$

# Emission components: not everything is Bremsstrahlung!

(and not everything is Fe-K....)

- Continuum

- Bremsstrahlung

- from all ions, not only hydrogen

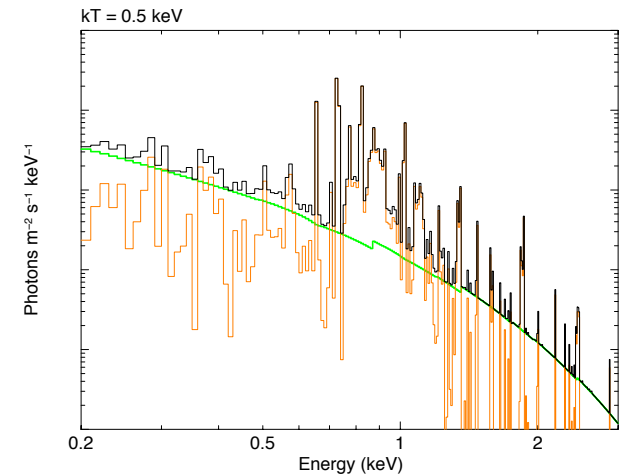
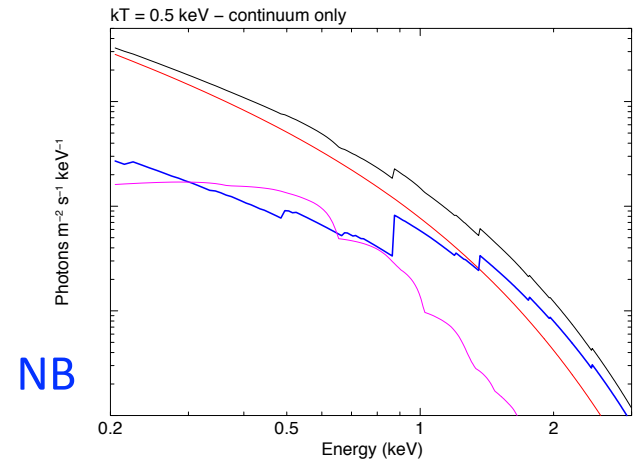
- Radiative Recombination  
Continuum (RRC)

- narrow, line-like for PIE plasmas

- Two Photon emission

- Lines

- Can dominate the flux at lower  
temperatures





# Absorption components

- Continuum "edges"
  - Easy to find with low-resolution instruments
  - Broad-band
- Absorption lines
  - Much more sensitive to detect low columns of plasma
  - Needs high-resolution
- EXAFS (Extended X-ray Absorption Fine Structure)
  - Tracer for solid state structure (dust)
  - Continuum wiggles near absorption edges

Now where are the atomic data and processes?

# Now where are the atomic data and processes?

- *For full plasma model, need many (12+) atomic processes:*
  - Collisional ionisation
  - Collisional excitation
  - Resonant excitation
  - Dielectronic recombination
  - Radiative transition probabilities
  - Auto-ionisation rates
  - Radiative Recombination rates
  - Photoionisation cross sections
  - Escape factors
  - Line energies
  - Charge exchange cross sections
  - Proton excitation
  - Etc.
- *Each process has its own intricacies and (atomic) data*

# Plasma codes & models

Code	Applicable	Notes
Raymond-Smith	CIE	Deprecated, use APEC
APEC/ATOMDB	CIE, NEI, CX	
Chianti	CIE	Widely used for Sun
Mekal	CIE, NEI	Deprecated, use SPEX
SPEX	CIE, NEI, PIE, CX	
XSTAR	PIE mainly	Evolved from X-ray band
Cloudy	PIE mainly	Evolved from optical/UV

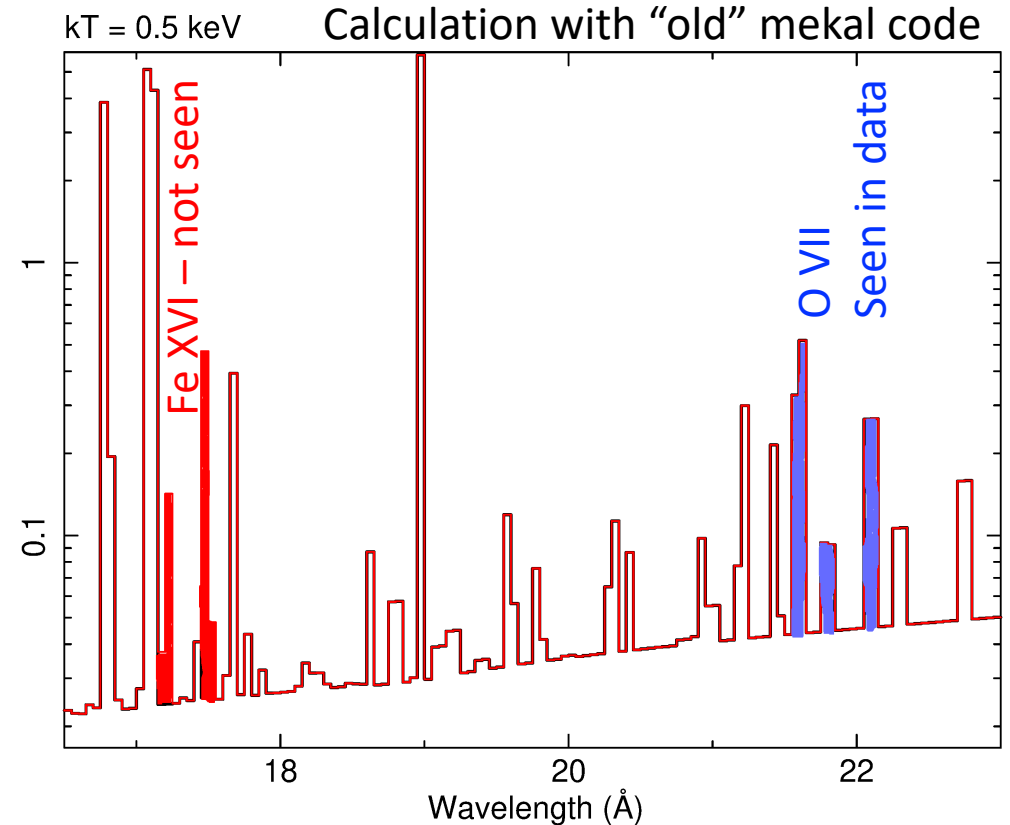
- All codes contain atomic data and algorithms to produce spectra
- Different techniques:
  - on the fly or pre-calculated
  - Original data or approximated data
  - Not always all processes included
- Level of modernity data can differ from code to code and process to process

# All things can be important

## Real example:

- “old” (pre-2000) mekal code had typo in **Fe XVI** lines (10x too strong) [not important for CCD but matters for grating]
- For RGS band, **Fe XVI** “coldest” Fe ion
- Line not seen in spectra, but predicted
- → Make emission measure at low T lower in the model
- **O VII** formed at same temperatures
- → Make **O abundance** higher
- → Strong bias

Most codes had/have similar “glitches”



# Analytical versus numerical

- Students learn to solve Schrödinger's equation  $i\hbar\partial\psi/\partial t = H\psi$  for Hydrogen analytically
- This is only case you can do this exact
- More than 1 electron → numerical methods
- Relativistic corrections important for e.g. Fe

# R-matrix versus distorted wave

- Two methods used frequently to calculate interactions with free electrons in complex ions:
- **R-matrix** is most accurate, but can deal with fewer levels
- **Distorted wave** (DW) is less accurate, but can deal with more levels
- Example DW codes: HULLAC (Klapisch et al.), FAC (M.F. Gu et al.)

# Now are the classical Bohr atom calculation useless?

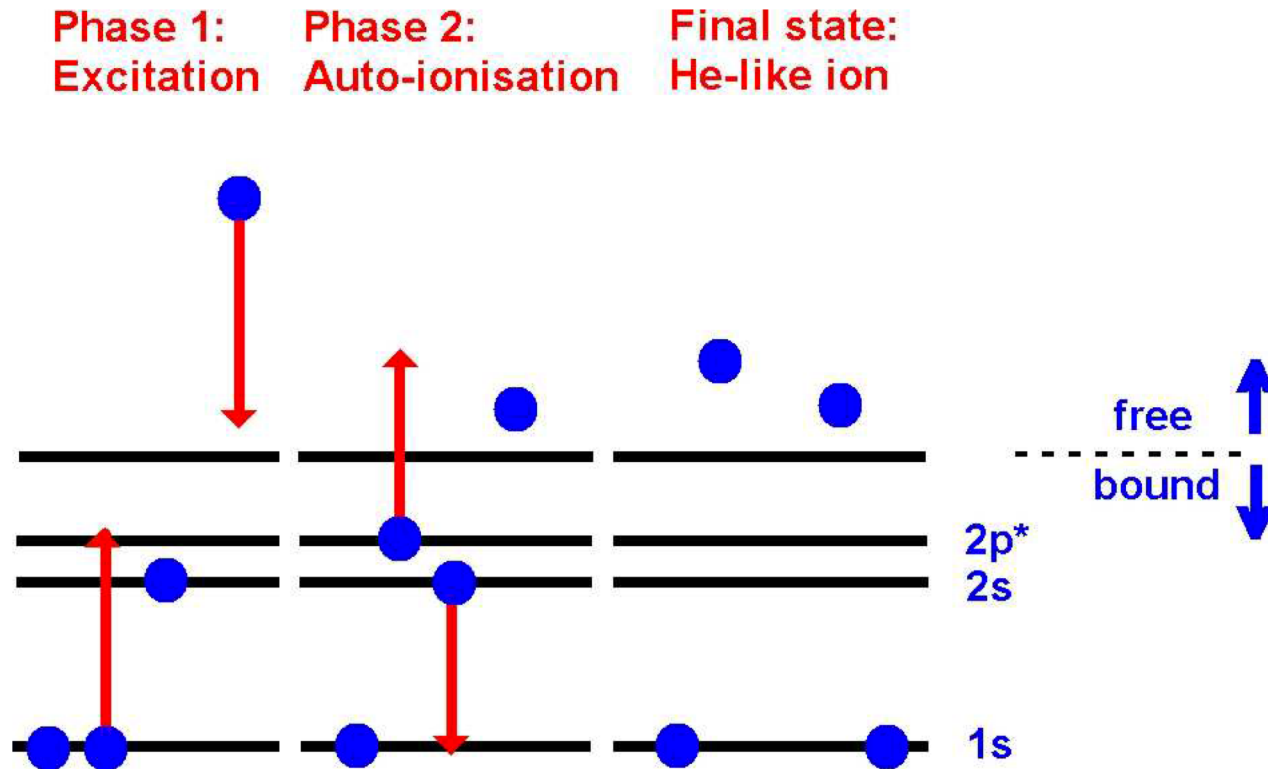
- *Not at all, can give you useful insights*
- with  $E_H=13.6$  eV,  $a_0=0.53$  Å,  $\alpha = 1/137$
- *Energy*     $E_n = -E_H Z^2 / n^2$ 
  - Higher charge, higher E
- *Size*     $r = n^2 a_0 / Z$ 
  - Higher charge, more compact
- *Orbital velocity*     $v/c = \alpha Z/n$ 
  - For  $Z=26$  (hydrogenic Fe) already significant relativistic effects ( $\sim 20\%$ )
  - Strong interaction if passing particle has this velocity



# Worked-out example: collisional ionisation

- Collision of a free electron with an atom can cause ionisation
- Several processes need to be accounted for:
  - Direct ionisation
  - Direct multiple ionisation (for high-E electrons)
  - Excitation autoionisation
- Highest rate if passing electron has similar speed as electron it kicks out

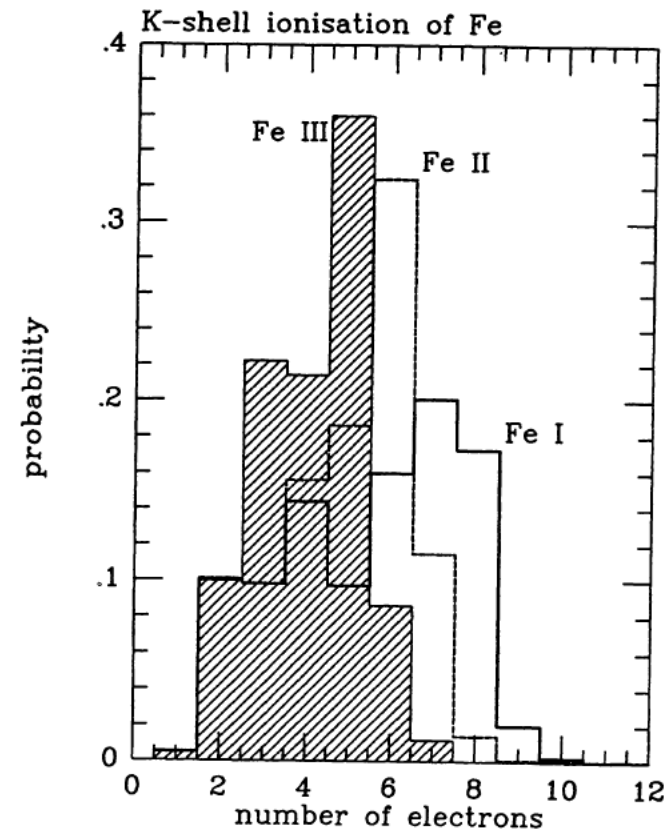
# Worked-out example: collisional ionisation



# Worked-out example: collisional ionisation

## *Cascades:*

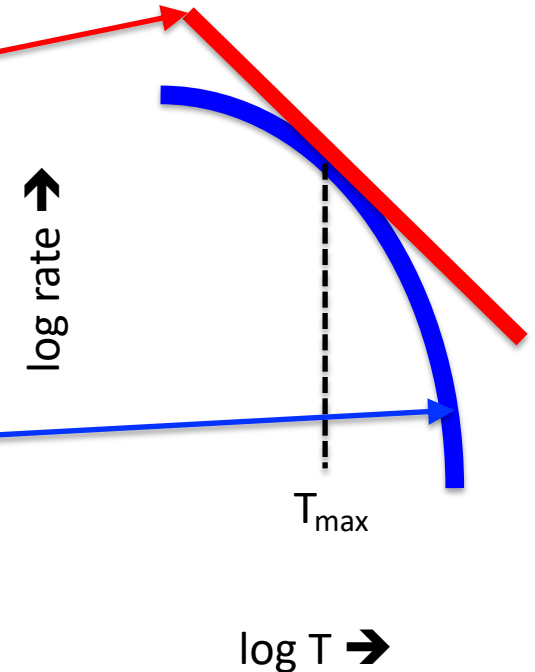
- One primary ionisation can lead to multiple ionisation
- Electrons from higher shells cascade down through fluorescent emission & Auger transitions
- Complex process to calculate because of many combinations



Kaastra & Mewe 1993

# Need for updates

- *Example:* Mewe approximated radiative recombination by local *power-law*
- *Okay for CIE* (dominated by collisional excitation) but:
- Large *deviations* for recombining / ionising plasma when true shape is used (Mao et al. 2016)
- Strong consequences for derived O, N abundances in clusters

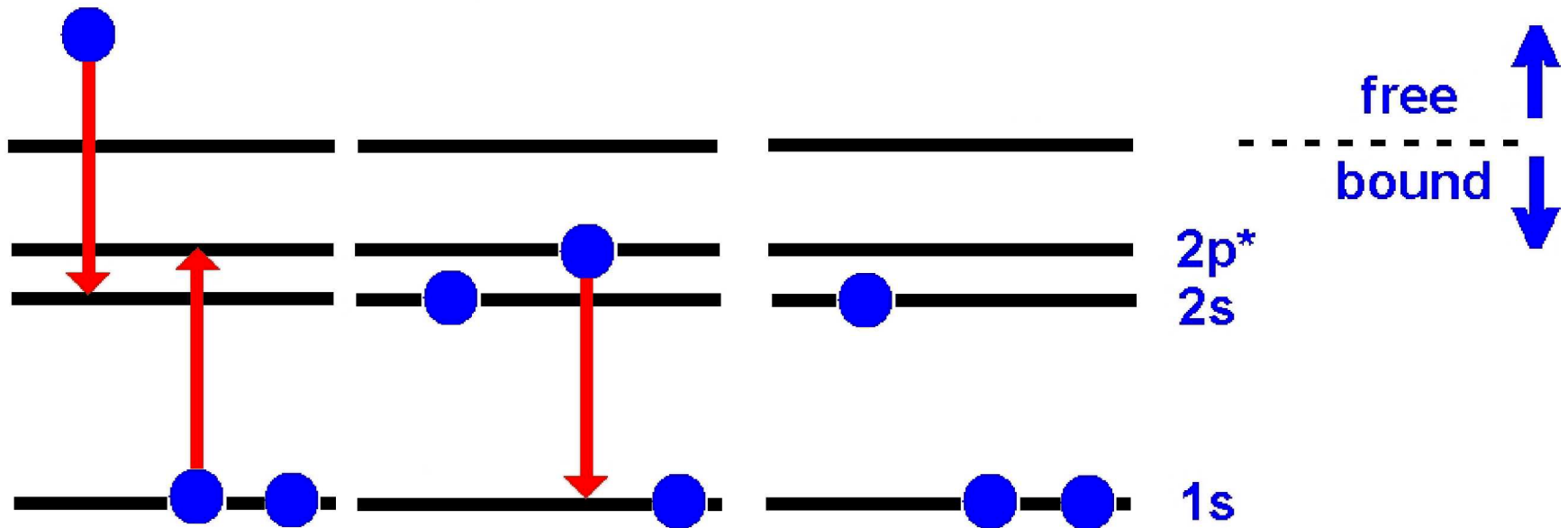


# Dielectronic recombination

**Phase 1:  
Excitation  
& capture**

**Phase 2:  
Radiative decay**

**Final state:  
Li-like ion**



# Why is dielectronic recombination hard to handle?

- Number of levels (combination of principal quantum number  $n$  and angular momentum  $\ell$ ) scales  $\propto n^2$  (because  $0 < \ell < n$ )
- In the DR process, doubly excited levels involved  $\rightarrow$  scales  $\propto n^4$
- For some ions, need to take into account levels up to  $n = O(10)$  to get accurate results

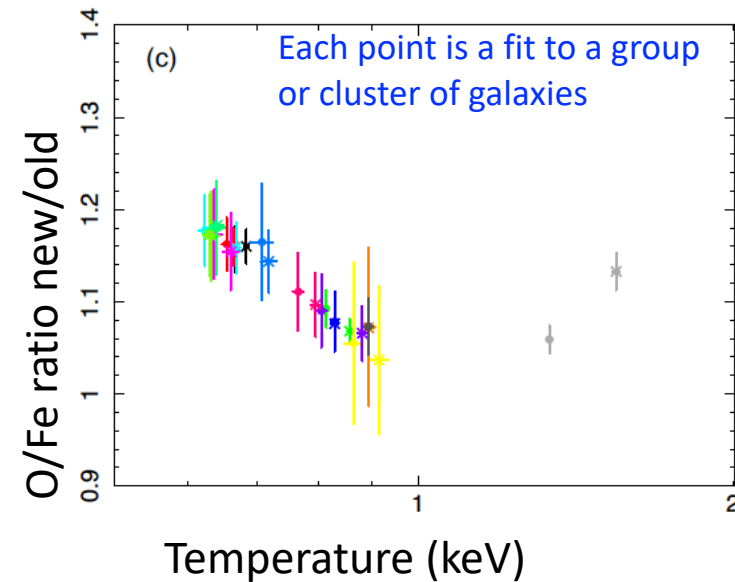
# Resonant excitation

- *First steps equal to dielectronic recombination:*
  - Free electron caught while bound electron excited (with energy conservation, no radiation)
  - This is doubly excited state (2 electrons in excited level)
- *Now the difference with DR:*
  - Auto-ionization, i.e. no radiation but one electron ejected, and other electron to lower level but not to the ground level
  - Ion is left in excited state
- Less energy needed for the initial free electron to start the process
- → Excitation (albeit resonant) possible below the threshold energy
- See next talk by Štofánová for one application

# Ongoing updates of SPEX: resonant excitation processes

(Liyi Gu et al. 2019)

- Update Fe L-shell ion spectra
- Focus on **Resonant Excitation** & **Dielectronic Recombination**
- Use FAC code with
  - 30.000 energy levels
  - 500.000 radiative transitions
  - 40.000 Auger rates
- Months of computation time
- Important astrophysical implications





# Final note on accuracies

- Few quantities calculated up to many digits (energies for H-like ions)
- Most quantities uncertain by several %, up to 10-20%
- Sometimes larger deviations (often human errors)
- Need to validate using independent models
- → APEC (Smith et al) & SPEX (Kaastra et al.):
  - Will not merge their codes
  - Are not competitors
  - Are friendly colleagues

# Conservative



If it's not a power law, it can't be true

# Modern times are coming



# Conclusions

- Atomic data matter
- Getting accurate atomic data is not trivial
- However, they are needed to avoid biased astrophysical results
- Atomic data intimately linked to the models in which they are applied
- Try to understand the basics of the models to appreciate your astrophysical results