



Abstract

We present a new model to simulate an energy spectrum of accretion-powered X-ray pulsars at very low accretion rates $\dot{M} \leq 5 \times 10^{15}$ g s⁻¹. We solve the polarized radiative transfer equation in the atmosphere of the neutron star taking into account magnetic Compton scattering and free-free processes. The structure of the atmosphere is obtained assuming energy balance and hydrostatic equilibrium. The model is able to explain the recent faint observations of accreting X-ray pulsars which show untypical bimodal spectral energy distribution with two humps around 5 keV and 30-40 keV. We argue that the high-energy component is the Wien hump due to saturated Comptonization in the hot dense upper layers of the neutron star atmosphere, modified by an imprinted cyclotron line. The low energy blackbody-like component results from the thermal irradiation from the deeper layers of the neutron star atmosphere, transferred by extraordinary photons.

Model description

We consider accretion onto strongly magnetized

neutron stars with rates corresponding to low lu-

minosities of $L \lesssim 10^{35}$ erg s⁻¹. At these accre-

tion rates no accretion column is formed. Accreted

matter falls freely and the final stopping occurs

within a thin layer of the neutron star atmosphere

by Coulumb collisions (Harding et al., 1984). We

model the emission from the polar cap by solving

the polarized radiative transfer in the neutron star



Figure 1: Schematic depiction of the polar cap model. atmosphere. We assume a plane-parallel slab of atmosphere with electron temperature and density varying along the z-coordinate parallel to the magnetic field \vec{B} and perpendicular to the surface (see Fig. 1). We tabulated synthetic spectra for a large set of parameter combinations to fit directly to observational data of low luminosity observations of X-ray pulsars. Hereafter we refer to our model as the **polcap** model.

Model parameters

M - mass accretion rate
r_0 - polar cap radius

 B_0 - surface magnetic field y_0 - atmosphere depth $T_{\rm BB}$ - seed photons temperature

Data analysis and results



Atmosphere structure and radiative transfer



We solve the energy balance and hydrostatic equations together within the neutron star atmosphere applying the approach from Zel'dovich & Shakura (1969). The equation of the energy balance can be written as

 $F_{\rm eff}\rho_{\rm e}/y_0 = \Lambda_{\rm B} + \Lambda_{\rm C},$ (1) where $F_{\rm eff} = L/(4\pi r_0^2), L$ is the luminosity of the polar cap determined by \dot{M} α is the electron density $r_{\rm e}$ is the

Figure 2: Atmosphere structure for depth $y_0 = 10$ and various \dot{M} . M, ρ_e is the electron density, r_0 is the polar cap radius, Λ_B is cooling by bremsstrahlung emission and Λ_C is cooling by Compton scattering.

In highly magnetized plasma of the neutron star atmosphere the radiation propagates in the form of two polarization normal modes which are usually referred to as ordinary (mode 2) and extraordinary (mode 1), which have significantly different scattering cross sections. We solve radiative transfer in two polarization modes

$$\frac{\cos^2\theta}{\kappa}\frac{\partial^2 u}{\partial z^2} - \kappa u + 4\pi \sum_{p'=1,2} \iint \frac{d^2\sigma_{pp'}}{dE'd\mu'}\frac{E}{E'}u\,dE'd\mu' + \alpha_{\rm ff}\bar{u}(E,T_{\rm e}) = 0 \tag{2}$$

for function $u = \frac{1}{2}(I(E, \mu, p, z) - I(E, -\mu, p, z))$ by the Feautrier method following the approach



Figure 4: Unfolded phase-averaged spectra of low-luminous observations: GX 304-1 at $L \sim 10^{34}$ erg s⁻¹ (top) and 1A 0535+262 at $L \sim 7 \times 10^{34}$ erg s⁻¹ (bottom). For both observations we assume a gravitational redshift of 0.3 which is an approximately redshift value near the neutron star surface. Absorption was also fixed to the $N_{\rm H} = 1.1 \times 10^{22}$ cm⁻². The red, blue and magenta crosses correspond to the *NuSTAR* FPMA /FPMB and *Swift*/XRT, respectively. The solid black lines show the fit by **polcap** model.

Conclusions and future work

The **polcap** model is presented, it can be used to describe the continuum shape of accreting X-ray pulsars faint observations. We argue that the atypical twocomponent spectra of such observations can be explained by radiative transfer in two polarization modes in a very hot optically thick medium. As a caveat, we note that the energy balance equation and radiative transfer are solved independently in the current version of the model, which leads to the fact that not all solutions

of Meszaros & Nagel (1985). Here κ is the total opacity, $\alpha_{\rm ff}$ is the free-free absorption coefficient and $d^2\sigma/dE'd\mu'$ is the differential scattering cross section, $\bar{u}(E, T_{\rm e})$ is the equilibrium photon density (Planck). The calculated spectra for two depths of the atmosphere y_0 are shown in the Fig. 3. Note the contribution of the different polarization modes to different energy ranges.



Figure 3: Energy flux from neutron star atmosphere for $\dot{M} = 10^{14} \text{ g s}^{-1}$, $B = 7.6 \times 10^{12} \text{ G}$, $r_0 = 10^4 \text{ cm}$, $kT_{\text{BB}} = 1.4 \text{ keV}$. Atmosphere depth is $y_0 = 6 \text{ g cm}^{-2}$ (a) and $y_0 = 10 \text{ g cm}^{-2}$ (b).

for atmosphere conserve energy. We will implement a more sophisticated scheme to obtain the solution, coupling radiative transfer and the energy balance equation as a next step. The good results shown above, however, are already very promising.

Acknowledgments & References

This work has been partially funded by DFG grant 1830Wi1860/11-1 and RSF grant 18-502-12025.

This research has made use of ISIS functions (ISISscripts) provided by ECAP/Remeis observatory and MIT (http://www.sternwarte.unierlangen.de/isis/).

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